# A MICRO-MANUAL FOR LISP - NOT THE WHOLE TRUTH 

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LISP data are symbolic expressions that can be either atoms of lists. Atoms are sit ings of letters and digits and other characters not otherwise used in LISP. A list consists of a left parenthesis followed by zero or more atoms or lists separated by spaces and ending with a right parenthesis. Examples: A, ONION, (), (A), (A ONION A), (PLUS 3 (TIMES X PI) 1), (CAR (QUOTE (A B))).

The LISP programming language is defined by rules whereby certain LISP expressions have other LISP expressions as values. The function called value that we will use in giving these rules is not part of the LISP language but rather part of the informal mothematical language uied to define LISP. Likewise, the italic letters $e$ and $a$ (sometimes with subscripts) denote LISP expressions, the letter $v$ (usually subscripted) denotes an atom serving as a variable, and the letter $f$ stands for a LISP expression serving as a function name.

1. value (QUOTE $e$ ) $=$ e. Thus the value of (QUOTE $A$ ) is $A$.
2. value (CAR $e$ ), where value $e$ is a non-empty list, is the first element of value e. Thus value (CAR (QUOTE (A B C))) $=\mathrm{A}$.
3. value (CDR e), where value $e$ is a non-empty tist, is the the list that remains when the first element of value $e$ is deleted. Thus value $(C D R(Q U O T E ~(A B C)))=(B C)$.
4. value (CONS el e2), is the list that results from prefixing value $e 1$ onto the list value e2. Thus value (CONS (QUOTE A) (QUOTE (BC))) $=\left(\begin{array}{l}\text { A C }\end{array}\right)$.
5. value (EQUAL e1 e2) is T if value $\mathrm{e} 1=$ value $e 2$. Otherwise, its value is NIL. Thus value (EQUAL (CAR (QUOTE (A B))) (QUOTE A)) - T.
6. value (ATOM e) = T if value $e$ is an atom; otherwise its value is NIL.
7. value $\left(\operatorname{COND}\left(p_{1} e_{1}\right) \ldots\left(p_{\mathrm{n}} e_{n}\right)\right)=$ value $\varepsilon_{\mathrm{i}}$, where $p_{\mathrm{i}}$ is the the first of the $p$ 's whose value is not NIL. Thus
value (COND ((ATOM (QUOTE A)) (QUOTE B)) ((QUOTE T) $(Q U O T E C))\rangle=B$.
8. An atom $v$, regarded as a variable, may have a value.
9. value ((LAMBDA $\left(v_{1} \ldots v_{n}\right)$ e) $\left.e_{1} \ldots e_{n}\right)$ is the same as value e but in an environment in which the variables $v_{1} \ldots v_{n}$ take the values of the expressions $e_{1} \ldots e_{n}$ in the original environment. Thus

[^0]10. Here's the hard one. value ((LABEL $f$ (LAMBDA $\left(v_{1} \ldots v_{n}\right)$ e)) $\left.e_{1} \ldots e_{n}\right)$ is the same as value ((LAMBDA $\left(v_{1} \ldots v_{n}\right)$ e) $e_{1} \ldots$ $\left.e_{n}\right)$ with the additional rule that whenever $\left(f a_{1} \ldots \dot{a}_{n}\right)$ must be evaluated, $f$ is replaced by (LABEL $f$ (LAMBDA $\left.\left.\left(v_{1} \ldots v_{n}\right) e\right\rangle\right)$. Lists beginning with LABEL define functions recursively.

This is the core of LISP, and here are more examples:
value $(\mathrm{CAR} \mathrm{X})=(\mathrm{AB}$ if value $\mathrm{X}=((\mathrm{AB}) \mathrm{C})$, and value ((LABEL FF (LAMBDA (X) (COND ((ATOM X) X) ((QUOTE
T) (FF (CAR X) $)$ ) $)$ ) $($ QUOTE $((\mathrm{A} \mathrm{B}) \mathrm{C})))=\mathrm{A}$. Thus ((LABEL FF (LAMBDA (X) (COND ((ATOM X) X) ((QUOTE T) (FF (CAR X) )) $)$ )), is the LISP name of a function ff such that ff $e$ is the first atom in the written form of $e$. Note that the list $f f$ is substituted for the atom FF twice.

Difficuit mathematical type exercise: Find a list e such that value $e=e$.

## Abbreviations

The above LISP needs some abbreviations for practical use.

1. The variables $T$ and NIL are permanently assigned the values $T$ and NIL, and NIL is the name of the null list ().
2. So as not to describe a LISP function each time it is used, we define it permanently by typing (DEFUN $f\left(\begin{array}{lll}v_{1} & \ldots & v_{n}\end{array}\right) e$ ). Thereafter ( $f e_{1} \ldots e_{n}$ ) is evaluated by evaluating $e$ with the variables $v_{1}, \ldots, v_{n}$ taking the values value $e_{1}, \ldots$, value $e_{n}$ respectively. Thus, after we define (DEFUN FF (X) (COND ((ATOM X) X) (T (FF (CAR X)) ) )), typing (FF (QUOTE ((A B) C) $)$ ), gets A from LISP.
3. We have the permanent function definitions
(DEFUN NULL (X) (EQUAL X NIL)) and
(DEFUN CADR (X) (CAR (CDR X)) ,
and similarly for arbitrary combinations of A and D.
4. (LIST $e_{1} \ldots e_{n}$ ) is defined for each $n$ to be (CONS $e_{1}$ (CONS ... (CONS $e_{\mathrm{n}}$ NIL) $)$ ).
5. (AND $p q$ ) abbreviates (COND ( $p q$ ) (T NIL)). ANDs with more terms are defined similarly, and the propositional connectives OR and NOT are used in abbreviating corresponding conditional expressions.

Here are more examples of LISP function definitions:
(DEFUN ALT (X) (COND ((OR (NULL X) (NULL (CDR X))) X) (T (CONS (CAR X) (ALT (CDDR X))) )) )
defines a function that gives alternate elements of a list starting with the first element. Thus (ALT (QUOTE (A B C D E) ) ) $=(\mathrm{A}$ C E).
(DEFUN SUBST (X Y Z) (COND ((ATOM Z) (COND ((EQUAL Z Y) X) (T Z)) ) (T (CONS (SUBST X Y (CAR Z)) (SUBST X Y (CDR Z) $)$ ) $)$ ),
where $Y$ is an atom, gives the result of substituting $X$ for $Y$ in $Z$. Thus
(SUBST (QUOTE (PLUS X Y)) (QUOTE V) QUOTE (TIMES $\mathbf{X} \mathbf{V}))\rangle=($ TIMES $X(P L U S X Y)$.

You may now program in LISP. Call LISP on a timesharing computer, define some functions, type in a LISP expression, and LISP will output its value on your terminal.

## THE LISP INTERPRETER WRITTEN IN LISP

The rules we have given for evaluating LISP expressions can themselves be expressed as a LISP function (EVAL a), where $e$ is an expression to be evaluated, and $a$ is a list of variable-value pairs. $a$ is used in the recursion and is often initially NIL. The long LISP expression that follows is just such an evaluator. It is presented as a single LABEL expressions with all auxiliary functions also defined by LABEL expressions internally, so that it references only the basic function of LISP and some of abbreviations like CADR and friends. It knows about all the functions that are used in its own definition so that it can evaluate itself evaluating some other expression. It does not know about DEFUNs or any features of LISP not explained in this micro-manual such as functional arguments, property list functions, input-output, or sequential programs.

The function EVAL can serve as an interpreter for LISP, and LISP interpreters are actually made by hand-compiling EVAL into machine language or by cross-compiling it on a machine for which a LISP system already exists.

The definition would have been easier to follow had we defined auxiliary functions separately rather than include them using LABEL. However, we would then have needed property list functions in order to make the EVAL self-applicable. These auxiliary functions are EVLIS which evaluates lists of expressions, EVCOND which evaluates conditional expressions, ASSOC which finds the value associated with a variable in the environment, and PAIRUP which pairs up the corresponding elements of two lists.

Here is EVAL.



[^0]:    value ((LAMBDA (X Y) (CONS (CAR X) Y)) (QUOTE (A B)) $(C D R ~(Q U O T E ~(C D))))=(A D)$.

